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Energy cost of walking and running at extreme uphill and downhill slopes

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Davide Susta, and Guido Ferretti. Energy cost of walking
and running at extreme uphill and downhill slopes. J
01177.2001.—The costs of walking (Cw) and running (Cr)
were measured on 10 runners on a treadmill inclined be-
tween −0.45 to +0.45 at different speeds. The minimum Cw
was 1.64 ± 0.50 J·kg⁻¹·m⁻¹ at a 1.0 ± 0.3 m/s speed on the
level. It increased on positive slopes, attained 17.33 ± 1.11
J·kg⁻¹·m⁻¹ at +0.45, and was reduced to 0.81 ± 0.37
J·kg⁻¹·m⁻¹ at −0.10. At steeper slopes, it increased to reach
3.46 ± 0.95 J·kg⁻¹·m⁻¹ at −0.45. Cr was 3.40 ± 0.24
J·kg⁻¹·m⁻¹ on the level, independent of speed. It increased
on positive slopes, attained 18.93 ± 1.74 J·kg⁻¹·m⁻¹ at
+0.45, and was reduced to 1.73 ± 0.36 J·kg⁻¹·m⁻¹ at −0.20.
At steeper slopes, it increased to reach 3.92 ± 0.81
J·kg⁻¹·m⁻¹ at −0.45. The mechanical efficiencies of walking
and running above +0.15 and below −0.15 attained those of
concentric and eccentric muscular contraction, respectively.
The optimum gradients for mountain paths approximated
0.20–0.30 for both gaits. Downhill, Cr was some 40% lower
than reported in the literature for sedentary subjects. The
estimated maximum running speeds on positive gradients
corresponded to those adopted in uphill races; on negative
gradients they were well above those attained in downhill
competitions; exercise; optimum path; maximum running speed

THE ENERGY COSTS OF LEVEL walking (Cw) and running
(Cr) in humans have been extensively investigated
(e.g., Refs. 4, 10, 12, 14, 15). Cw varies as a function of
the speed, showing a minimum value at ∼1.3 m/s. Cr is
independent of the speed. Both Cw and Cr depend on
the characteristics of the terrain, resulting higher on
soft than on hard ground (13, 27). Adding a 1-kg load
on the lower limbs increases Cr up to 7%, depending on
where masses are added (16). Cr is also affected by the
foot landing patterns, which allow a different efficiency
of leg muscles and tendons (2) and increase when
muscles are fatigued (5).

When walking or running on positive gradients, both
the minimum Cw and the Cr increase as a function of
the incline [up to +0.15 for running and up to +0.40 for
walking (14, 15)]. When negative gradients are applied,
both Cr and the minimum Cw attain their lowest
value at −0.10. Below this slope, and down to −0.20 for
running and to −0.40 for walking, minimum Cw and
Cr are negatively related to the incline, becoming
higher the lower the slope (14, 15). The range of run-
ing gradients (from −0.20 to +0.15), narrower than for
walking, was set by the aerobic power of the sub-
jects, none of whom was a professional long-distance
runner.

Margaria (14) introduced also the concept of “mech-
anical efficiency,” defined as the ratio of mechanical
work for vertical displacement to the energy expended.
He adopted the approximation of considering just the
mechanical potential work (and disregarding the ki-
etic one) because he assumed that beyond a given
gradient the rise (or descent) of the center of mass is
the prevailing contributor to the mechanical external
work. This assumption was supported by recent re-
search (19, 20), which set the ±0.15 gradient as the
threshold for pure positive and negative work in uphill
and downhill locomotion, respectively. At slopes above
+0.20, Margaria found that the efficiency of walking
was ∼0.25, i.e., close to that of concentric muscle con-
tractions (26). At slopes below −0.20, the mechanical
efficiency of walking was about −1.20, as for eccentric
muscular contractions (1). Margaria postulated that
this would have been the case also for running. Suc-
cessively, little attention was paid to the study of the
cost of locomotion at extreme slopes, despite the fact
that in recent years walking and running on mountain
paths became common practices in leisure time and
sport. Davies et al. (8) studied one subject running
downhill at −0.40; their results appear to agree with
Margaria’s hypothesis. To our knowledge, however, no
systematic study of Cr during downhill and uphill
running has been carried out so far.

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The aim of the present study was to determine $C_w$ and $Cr$ on men walking and running on a treadmill at slopes ranging from $-0.45$ to $+0.45$, to encompass, especially for running, a wider range of slopes than in any previous study. In addition, we compared the maximum estimated running speeds as a function of the gradient, with the top performances in just-uphill and just-downhill fell running races.

**METHODS**

**Subjects.** After local ethical approval, 10 subjects were admitted to the study [men age 32.6 $\pm$ 7.5 yr, body mass 61.2 $\pm$ 5.7 kg, maximal $O_2$ consumption $(\dot{V}_{O_2, max})$ 68.9 $\pm$ 3.8 ml·min$^{-1}$·kg$^{-1}$]. They were all elite athletes practicing endurance mountain racing.

**Methods.** The $O_2$ consumption ($\dot{V}_{O_2}$) and $CO_2$ output ($\dot{V}_{CO_2}$) at rest and at the exercise steady state were measured by the standard open-circuit method. Expired air was collected in Douglas bags and analyzed for gas composition by use of $O_2$ and $CO_2$ analyzers (Leybold Haereus) and for volume by using a dry gas meter (Singer). $V_{O_2}$ and $V_{CO_2}$ were then calculated and expressed in m$^3$·d$^{-1}$. $\dot{V}_{O_2}$ was measured by an incremental exercise test on the treadmill.

Heart rate was measured continuously by cardiograph (Polar), and blood lactate concentration was determined during mountain racing. Before a test was performed, the speed of spontaneous transition was carried out at the lowest investigated speed, was 0.69 m/s. The average minimum $C_w$ was $0.81$ $\pm$ $0.37$ J·kg$^{-1}$·m$^{-1}$ at the speed of 0.69 m/s. The average minimum $C_w$ was $17.3$ $\pm$ $1.11$ J·kg$^{-1}$·m$^{-1}$ at a speed of 1.0 $\pm$ 0.3 m/s. The minimum $C_w$ was measured by an incremental exercise test on the treadmill.

Metabolic parameters of running at the highest tested speed as a function of the speed, were investigated in such a manner that the speed of spontaneous transition was set equal to the spontaneous transition speed. For the successive two trials at faster speeds, an increment of 0.56 m/s was usually imposed. This increment was reduced at high positive slopes, to cope with the need of performing submaximal exercise trials. However, in some cases, a test was interrupted without completing the three running speeds, if blood lactate accumulation was higher than 4 mM. This happened particularly at the highest positive slopes, and on four subjects running could not be performed at slopes of $+0.40$ and $+0.45$.

**RESULTS**

$\dot{V}_{O_2}$ increased as a function of speed from 0.69 m/s onward during walking. During running, it increased linearly with the speed. At each speed, it was higher the higher the uphill gradient. The $\dot{V}_{O_2}$ values observed at the highest tested speed on the level and during uphill locomotion at each slope are reported in Table 1, together with the corresponding heart rate and blood lactate values.

The $C_w$ on the level was $1.85$ $\pm$ $0.57$ J·kg$^{-1}$·m$^{-1}$ at the speed of 0.69 m/s. The average minimum $C_w$ was $1.64$ $\pm$ $0.50$ J·kg$^{-1}$·m$^{-1}$ at a speed of 1.0 $\pm$ 0.3 m/s. The minimum $C_w$ was plotted in Fig. 1A as a function of the speed. During uphill walking, the minimum $C_w$ increased with the slope. At the slope of $+0.45$, minimum $C_w$ was $17.3$ $\pm$ $1.11$ J·kg$^{-1}$·m$^{-1}$ at the speed of 0.69 m/s for all subjects. During downhill walking, the minimum $C_w$ attained its lowest value (0.81 $\pm$ 0.37 J·kg$^{-1}$·m$^{-1}$) at the slope of $-0.10$ at the average speed of 3.14 $\pm$ 0.22 m/s. At slopes below $-0.10$, it progressively increased. At $-0.45$, it was 3.46 $\pm$ 0.95 J·kg$^{-1}$·m$^{-1}$.

$Cr$ on the level was $3.40$ $\pm$ $0.24$ J·kg$^{-1}$·m$^{-1}$, independent of speed. The average $Cr$ at the investigated speeds is plotted in Fig. 1B as a function of the speed. $Cr$ increased with the slope uphill to attain 18.93 $\pm$ 1.74 J·kg$^{-1}$·m$^{-1}$ at $+0.45$. This value was only 9.2 $\pm$ 2.6% higher than the minimum $C_w$ at the same slope, whereas on the level $Cr$ was 107.3 $\pm$ 49.8% higher than the minimum $C_w$. During downhill running, $Cr$ decreased and attained its lowest value at $-0.20$ (1.73 $\pm$ 0.36 J·kg$^{-1}$·m$^{-1}$). At lower slopes it increased again. At $-0.45$, it was 3.92 $\pm$ 0.81 J·kg$^{-1}$·m$^{-1}$. The average minimum $C_w$ and the $Cr$ observed at each investigated slope are summarized in Table 2.

**Table 1. Metabolic parameters of running at the highest tested speed at each uphill slope**

<table>
<thead>
<tr>
<th>Speed, m/s</th>
<th>$\dot{V}_{O_2}$, ml·kg$^{-1}$·min$^{-1}$</th>
<th>Heart Rate, min$^{-1}$</th>
<th>Lactate, mM</th>
</tr>
</thead>
<tbody>
<tr>
<td>-0.45</td>
<td>1.63 $\pm$ 0.40</td>
<td>23.2 $\pm$ 3.3</td>
<td>131 $\pm$ 26</td>
</tr>
<tr>
<td>-0.40</td>
<td>1.86 $\pm$ 0.30</td>
<td>23.5 $\pm$ 2.3</td>
<td>122 $\pm$ 26</td>
</tr>
<tr>
<td>-0.35</td>
<td>2.14 $\pm$ 0.22</td>
<td>22.2 $\pm$ 3.0</td>
<td>116 $\pm$ 23</td>
</tr>
<tr>
<td>-0.30</td>
<td>2.52 $\pm$ 0.58</td>
<td>22.0 $\pm$ 3.1</td>
<td>113 $\pm$ 17</td>
</tr>
<tr>
<td>-0.20</td>
<td>2.84 $\pm$ 0.39</td>
<td>18.9 $\pm$ 2.6</td>
<td>100 $\pm$ 13</td>
</tr>
<tr>
<td>-0.10</td>
<td>3.08 $\pm$ 0.26</td>
<td>23.3 $\pm$ 5.7</td>
<td>101 $\pm$ 8</td>
</tr>
<tr>
<td>0.00</td>
<td>3.13 $\pm$ 0.22</td>
<td>35.5 $\pm$ 2.7</td>
<td>125 $\pm$ 15</td>
</tr>
<tr>
<td>0.10</td>
<td>2.90 $\pm$ 0.27</td>
<td>53.0 $\pm$ 8.6</td>
<td>158 $\pm$ 11</td>
</tr>
<tr>
<td>0.20</td>
<td>2.11 $\pm$ 0.27</td>
<td>56.2 $\pm$ 4.4</td>
<td>168 $\pm$ 13</td>
</tr>
<tr>
<td>0.30</td>
<td>1.46 $\pm$ 0.12</td>
<td>58.4 $\pm$ 2.9</td>
<td>169 $\pm$ 10</td>
</tr>
<tr>
<td>0.35</td>
<td>1.18 $\pm$ 0.14</td>
<td>57.5 $\pm$ 2.6</td>
<td>167 $\pm$ 12</td>
</tr>
<tr>
<td>0.40</td>
<td>0.99 $\pm$ 0.10</td>
<td>55.5 $\pm$ 1.2</td>
<td>169 $\pm$ 15</td>
</tr>
<tr>
<td>0.45</td>
<td>0.89 $\pm$ 0.10</td>
<td>52.1 $\pm$ 4.2</td>
<td>167 $\pm$ 14</td>
</tr>
</tbody>
</table>

Values are means $\pm$ SD. $\dot{V}_{O_2}$ is the overall steady-state oxygen consumption.
The vertical cost of walking and running (J·kg\(^{-1}\)·m\(^{-1}\)) is defined as the energy expenditure to walk or to run a distance that corresponds to a vertical displacement of 1 m. It is plotted in Fig. 2A for walking and in Fig. 2B for running. The vertical cost decreased during uphill running to attain a minimum value of 44.9 ± 3.8 J·kg\(^{-1}\)·m\(^{-1}\) in the slope range of 0.20–0.40. During downhill running, the vertical cost decreased, to attain a minimum of 9.2 ± 1.7 J·kg\(^{-1}\)·m\(^{-1}\) in the slope range from −0.20 to −0.40.

The mechanical efficiency for running is shown in Fig. 3. For uphill slopes steeper than +0.15, they were 0.243 ± 0.012 and 0.218 ± 0.06 for walking and running, respectively. For downhill slopes steeper than −0.15, they were −1.215 ± 0.184 and −1.062 ± 0.056, respectively.

**DISCUSSION**

The present study demonstrates that uphill Cw and Cr data are directly proportional to the slope above +0.15, compatibly with a mechanical efficiency of 0.22–0.24. During downhill locomotion, Cw and Cr show a linear negative relation with the slope below −0.15, compatibly with a mechanical efficiency of −1.06 to −1.21. These results fully support the hypothesis of Margaria and co-workers (14, 15), according to which the efficiency of uphill locomotion at sufficiently high slopes ought to become equal to that of concentric muscular work, whereas downhill efficiency ought to become close to that of negative work, i.e., −1.2 (1). It is important to remember that the mechanical efficiency mentioned so far is calculated by dividing the potential energy changes by the metabolic consumption; thus those values are reliable only when the kinetic energy changes are incomparably smaller and when only positive or only negative work is associated to the motion of the body center of mass. In Fig. 3, the arrow defines the gradient range ±0.15, within which the mechanical external work of walking (19) and running (20) is still contributed by a mixture of positive and negative work. For steeper positive gradients, the 0.25 efficiency value implies that all the work be done to lift the body: only positive work is done in both gaits, and the descending phase of the pendulum-like and bouncing ball (6) mechanisms of walking and running is lost. By analogy, for steeper negative gradients, the −1.2 efficiency value implies that only negative work is done in both gaits and that the ascending phase of the pendulum-like and bouncing ball (6) mechanisms of walking and running is lost. Because either mechanism requires both an ascending and a descending phase of the trajectory to allow for the recovery of mechanical energy, the concept (21) that walking and running, when operated at gradients steeper than the ±0.15 range, lose the pendulum-like and the bouncing-ball mechanism, respectively, is reinforced. If this is so, and if we consider how Cw and Cr become close at the steepest gradients, we wonder whether it is legitimate to speak of “walking” or “running” at the steepest slopes. A biomechanical study of walking and running on steep gradient would be required for an appropriate characterization of the gait and for a clear identification, from the measure of contact times, of the transition from a walkinglike to a runninglike gait when the differences between walking and running tend to disappear.
A comparison of the present results with those from previous studies is attempted in all the illustrated figures. Despite of the different methodology involved, the spontaneous speed of transition between walking and running is similar to the one reported in a subset of gradients (21). Although Cw is very similar to what previously reported (14), as shown in Fig. 1A, Cr seems to resemble the reported data (14, 15, 20) only at level and uphill gradients (see Fig. 1B). This suggests that the athletes presently investigated, specifically trained in fell-running, developed a more economical style than nonathletic subjects during descent. Because little can be done on the path of the center of mass at extreme slopes that could reduce the overall mechanical work, a possible explanation of the greater economy could be the decrease in cocontractions needed to stabilize the descent.

To focus on the optimization of the vertical cost of walking and running on slopes, a new index, the cost of walking and running vertically (Cw vert and Cr vert), has been defined as the cost of walking and running vertically arranged as a function of the gradient, from the present investigation ( ), and from Minetti (18), where reprocessed data from Margaria (14, 15) were presented.

Fig. 2. Metabolic energy cost of walking (A) or running (B), expressed per unit of vertical distance (m vert) as a function of the gradient, from the present investigation ( ), and from Minetti (18), where reprocessed data from Margaria (14, 15) were presented.

Table 2. Minimum cost of walking and cost of running at the indicated slopes on the treadmill

<table>
<thead>
<tr>
<th>Slope</th>
<th>Cw</th>
<th>Cr</th>
</tr>
</thead>
<tbody>
<tr>
<td>-0.45</td>
<td>n = 10</td>
<td>n = 10</td>
</tr>
<tr>
<td>3.46 ± 0.95</td>
<td>3.92 ± 0.81</td>
<td></td>
</tr>
<tr>
<td>0.40</td>
<td>n = 10</td>
<td>n = 9</td>
</tr>
<tr>
<td>3.23 ± 0.59</td>
<td>3.49 ± 0.47</td>
<td></td>
</tr>
<tr>
<td>-0.35</td>
<td>n = 10</td>
<td>n = 10</td>
</tr>
<tr>
<td>2.65 ± 0.68</td>
<td>2.81 ± 0.54</td>
<td></td>
</tr>
<tr>
<td>-0.30</td>
<td>n = 10</td>
<td>n = 30</td>
</tr>
<tr>
<td>2.18 ± 0.67</td>
<td>2.43 ± 0.50</td>
<td></td>
</tr>
<tr>
<td>-0.20</td>
<td>n = 10</td>
<td>n = 24</td>
</tr>
<tr>
<td>1.30 ± 0.48</td>
<td>1.73 ± 0.36</td>
<td></td>
</tr>
<tr>
<td>-0.10</td>
<td>n = 10</td>
<td>n = 24</td>
</tr>
<tr>
<td>0.81 ± 0.37</td>
<td>1.93 ± 0.45</td>
<td></td>
</tr>
</tbody>
</table>

Values are means ± SD. Cw, cost of walking; Cr, cost of running.

A comparison of the present results with those from previous studies is attempted in all the illustrated figures. Despite of the different methodology involved, the spontaneous speed of transition between walking and running is similar to the one reported in a subset of gradients (21). Although Cw is very similar to what previously reported (14), as shown in Fig. 1A, Cr seems to resemble the reported data (14, 15, 20) only at level and uphill gradients (see Fig. 1B). This suggests that the athletes presently investigated, specifically trained in fell-running, developed a more economical style than nonathletic subjects during descent. Because little can be done on the path of the center of mass at extreme slopes that could reduce the overall mechanical work, a possible explanation of the greater economy could be the decrease in cocontractions needed to stabilize the descent.

The vertical cost of walking and running on slopes has been introduced (18) to focus on the optimization of the work done for the vertical displacement of the body during locomotion as a function of the gradient. Data are from the present investigation, from Margaria (14, 15) and from Minetti (20). Double-headed arrow parallel to the x-axis defines the gradient range where the external work of locomotion is contributed by a combination of positive and negative work. Note that the y-axis scale reports the absolute value of efficiency: the sign ought to be negative for downhill locomotion, positive for uphill locomotion.

Fig. 3. Mechanical efficiency of the work done for the vertical displacement of the body during locomotion as a function of the gradient. Data are from the present investigation, from Margaria (14, 15) and from Minetti (20). Double-headed arrow parallel to the x-axis defines the gradient range where the external work of locomotion is contributed by a combination of positive and negative work. Note that the y-axis scale reports the absolute value of efficiency: the sign ought to be negative for downhill locomotion, positive for uphill locomotion.
mountain paths. It was concluded that for walking the gradient minimizing the metabolic cost should be \(~0.25–0.28\), both uphill and downhill. This concept is essentially supported by the present results (see Fig. 2A), though the minimum vertical cost for downhill walking looks broader than expected. In running, it was previously impossible to estimate such an optimum gradient, mainly because of the limited slope range available (see Fig. 2B). The present work, by extending the slope range to \(\pm 0.45\), shows that it is similar to the one for walking, despite the broader minima: these probably reflect the athletes' ability to perform in very different conditions (see Fig. 2B). Particularly at downhill gradients, at which athletes report a 30–50% reduction in the vertical cost, a better technique allowing a greater recovery of elastic energy could be responsible for the increased economy.

From the results of the present investigation, it is now possible 1) to estimate the maximum (aerobic) running speed as a function of both positive and negative gradient and 2) to compare it with the best results from uphill-only and downhill-only races, available from official mountain Federation of Sport at Altitude competitions.

As indicated in METHODS, the metabolic energy cost (Cr\(_{v,i}\), in J·kg\(^{-1}\)·m\(^{-1}\)) of running a unit distance at any given speed and gradient has been calculated as

\[
Cr_{v,i} = \frac{E_{\max,i}}{v_i}
\]

where \(E_{\max,i}\) is the net metabolic power (W/kg) measured during the experiments. It is widely known, and it was confirmed by this study too, that Cr\(_{v,i}\) changes at each gradient \(i\) (see Fig. 2), but it is quite constant at all running speeds within every single gradient; thus the index \(v\) can be removed from that symbol. Such a peculiar characteristic of running, so different from other gaits such as walking, allows estimation at each gradient of the maximum running speed (\(v_{\max,i}\), m/s).

The previous equation can be expressed as

\[
v_{\max,i} = \frac{E_{\max,i}}{Cr_i}
\]

where \(E_{\max,i}\) is the maximum oxygen consumption (in W/kg) of the subjects group (11). Because only a fraction of the maximum metabolic power \(E_{\sub max,i}\) can be used to sustain aerobic exercise in long-lasting events (see below), and this last parameter is obviously independent from \(i\), the last equation becomes

\[
v_{\max,i} = \frac{E_{\sub max}}{Cr_i}
\]

Once the numerator in Eq. 2 has been set, say 18 W/kg, the maximum running speed is obtained, as shown by the thick curve in Fig. 4. Those estimates linearly scale with the maximum aerobic power or its sustainable fraction, as indicated by the other two curves in Fig. 4. The same applies to the calculation of the maximum vertical speed of running (\(v_{\max,\text{vert}}\), m\(\text{vert}/\text{s}\)), as obtained from

\[
v_{\max,\text{vert},i} = v_{\max,i} \sin(\arctan|i|)
\]

and shown in Fig. 5 for three levels of available metabolic power. For instance, \(v_{\max,\text{vert}}\) was estimated to be \(~2.1\) and \(0.4\) m\(\text{vert}/\text{s}\) for downhill \((i = -0.25)\) and uphill \((i = +0.25)\) gradients, respectively, for a \(V_{\text{O2 sub max}}\) equal to 18 W/kg.

To compare these estimates to the real running speeds, as observed during competition, we could not expect the race results to follow a single curve in Fig. 4 or 5, because, even assuming that all the athletes report the same maximum aerobic power, two other main variables affect the available metabolic power during the event, even for the same average gradient.
In fact, it is known that the available fraction of $\dot{V}_\text{O}_2 \max$ ($E\dot{E}_\text{max}$) depends on the exercise duration ($\text{fract}_{\text{duration}}$) (23) and on the altitude above sea level ($\text{fract}_{\text{altitude}}$) (7) at which the exercise is performed, and both effects are strongly involved in gradient running events. Thus we could write

$$E\dot{E}_{\text{sub max}} = E\dot{E}_\text{max} \cdot \text{fract}_{\text{duration}} \cdot \text{fract}_{\text{altitude}}$$  \hfill (6)

where

$$\text{fract}_{\text{duration}} = \frac{940 - t_{\text{event}}}{60 \cdot 1000}$$  \hfill (7)

adapted from Saltin (24), where $t_{\text{event}}$ is the event duration, and

$$\text{fract}_{\text{altitude}} = 1 - 11.7 \cdot 10^{-9} \cdot \text{altitude}^2 - 4.01 \cdot 10^{-6} \cdot \text{altitude}$$  \hfill (8)

from Cerretelli (7). In Eqs. 7 and 8, $t_{\text{event}}$ and altitude are expressed in seconds and meters, respectively.

Table 3 reports data available from the Internet about some only-uphill and only-downhill running races. When the event best time, the distance traveled, the difference in altitude and, sometimes, the maximum altitude reached are known, the average gradient and the predicted $v_{\text{max}}$ and $v_{\text{max vert}}$ can be calculated by using Eqs. 3-8. In the sample of events shown in the table, the striking result is the very close match between predicted and measured maximum vertical speed in uphill running (their ratio is $0.950 \pm 0.130$), whereas predicted speed for downhill races overestimates the measured one by a factor of 3 (their ratio is $3.446 \pm 1.324$), as shown in Fig. 6.

Such a discrepancy is astonishingly too large to be explained in terms of differences in muscular efficiency only. In downhill competitions, athletes do not seem to use the full amount of the available aerobic power for increasing their speed. The reasons should be methodological and/or inherent in reproducing an outdoor condition in the laboratory. In the following, a list of potential determinants of such a speed choice is re-

<table>
<thead>
<tr>
<th>Location, vertical km</th>
<th>Distance, km</th>
<th>Duration, s</th>
<th>Height, m</th>
<th>Altitude, m</th>
<th>Gradient</th>
<th>$v_{\text{vert}}$ Predicted, mvert/s</th>
<th>$v_{\text{vert}}$ Predicted, mvert/s</th>
<th>$v_{\text{vert}}$ Predicted/Measured</th>
<th>$v_{\text{O}_2}$ Predicted, ml·kg$^{-1}$·min$^{-1}$</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Up</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Mt. Cameroon up</td>
<td>2.9</td>
<td>2,132</td>
<td>981</td>
<td>4,095</td>
<td>0.360</td>
<td>0.460</td>
<td>0.407</td>
<td>0.884</td>
<td>62.4</td>
</tr>
<tr>
<td>Mt. Washington</td>
<td>18.0</td>
<td>12,600</td>
<td>3,400</td>
<td>4,095</td>
<td>0.192</td>
<td>0.270</td>
<td>0.330</td>
<td>1.225</td>
<td>39.7</td>
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<td>Mt. Tennant</td>
<td>12.2</td>
<td>3,500</td>
<td>1417</td>
<td>4,095</td>
<td>0.117</td>
<td>0.405</td>
<td>0.318</td>
<td>0.786</td>
<td>68.1</td>
</tr>
<tr>
<td>Mt. Ainslie</td>
<td>6.6</td>
<td>2,198</td>
<td>700</td>
<td>4,095</td>
<td>0.107</td>
<td>0.318</td>
<td>0.312</td>
<td>0.980</td>
<td>56.7</td>
</tr>
<tr>
<td>Dolomites</td>
<td>2.2</td>
<td>620</td>
<td>230</td>
<td>4,095</td>
<td>0.105</td>
<td>0.371</td>
<td>0.319</td>
<td>0.859</td>
<td>65.8</td>
</tr>
<tr>
<td>Cervinia km</td>
<td>3.5</td>
<td>2,544</td>
<td>1,000</td>
<td>4,095</td>
<td>0.298</td>
<td>0.393</td>
<td>0.409</td>
<td>1.042</td>
<td>53.2</td>
</tr>
<tr>
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<td>10.0</td>
<td>5,004</td>
<td>1,702</td>
<td>4,095</td>
<td>0.173</td>
<td>0.340</td>
<td>0.359</td>
<td>1.056</td>
<td>50.3</td>
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<tr>
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<td>1,480</td>
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<td>0.099</td>
<td>0.319</td>
<td>0.287</td>
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<td>58.8</td>
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<td>Mean ± SD</td>
<td></td>
<td></td>
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<td></td>
<td></td>
<td>0.144</td>
<td>0.320</td>
<td>0.309</td>
<td>0.967</td>
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<tr>
<td><strong>Down</strong></td>
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<td></td>
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<td></td>
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<tr>
<td>Kinabalu down</td>
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<td>-2,205</td>
<td>4,095</td>
<td>-0.226</td>
<td>0.645</td>
<td>3.250</td>
<td>5.041</td>
<td>19.6</td>
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<td>4,500</td>
<td>-2,200</td>
<td>4,301</td>
<td>-0.105</td>
<td>0.489</td>
<td>1.758</td>
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<td>2,280</td>
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<td>4,165</td>
<td>-0.168</td>
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<td>1.785</td>
<td>1.884</td>
<td>32.7</td>
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<td>-3,807</td>
<td>4,810</td>
<td>-0.245</td>
<td>0.690</td>
<td>3.001</td>
<td>4.351</td>
<td>20.3</td>
</tr>
<tr>
<td>Mt. Cameroon down</td>
<td>18.0</td>
<td>3,717</td>
<td>-3,400</td>
<td>4,095</td>
<td>-0.192</td>
<td>0.915</td>
<td>2.157</td>
<td>2.358</td>
<td>28.4</td>
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<tr>
<td>Mean ± SD</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>3.446 ± 1.324</td>
<td>26.5 ± 6.2</td>
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</tr>
</tbody>
</table>

The assumption of a maximal rate of aerobic energy expenditure of 22.6 W/kg was made.

![Fig. 6. Predicted maximum vertical speed vs. actual vertical speed as reported from mountain-running competitions. Predictions were made according to Eqs. 3–8 and the data regarding distance, duration, and average altitude. Only uphill (gray circles) and only downhill (©) competitions are reported. The assumption of a maximal rate of aerobic energy expenditure of 22.6 W/kg was made.](image-url)
ported in descending order for relevance (and likelihood).

1) During downhill running, other criteria such as the maintenance of a reasonable safety factor could be operating to minimize joint and tissue injuries. It is likely that at extreme downhill slopes muscles could not cope with the tendency of the body to accelerate, rather than maintaining a constant speed throughout a controlled constant braking. That would result in the lack of the fine motor control needed to maintain body trajectory on a rough and slippery terrain. Among the associated risks is the iliotibial band friction syndrome, more frequent in downhill running because the knee flexion angle at foot strike is reduced (22, 23), and the intravascular hemolysis due to foot impact forces (17) which should proportionally increase Cr, and increase in EMG activity (9) take place.

This analysis points out how in competitive downhill running, differently from the uphill situation and many other sport activities, “power without control is nothing.” To verify the relative contribution and the relevance of the hypothesized list of determinants for choosing to run slower than metabolically possible at extreme downhill gradients, further experiments on the capacity of the neuromusculoskeletal system to brake the body motion are needed.

In conclusion, the present study extends the previous literature about the economy of locomotion to include extreme slopes up to ±0.45, an unprecedented range particularly for running. The results show that 1) the minimum in energy cost is similar in walking and running at ~0.10–0.20 downhill gradient; 2) the optimum gradient for mountain paths is close to 0.20–0.30, both uphill and downhill, for the two gaits; 3) a better progression economy is expected in mountain-running athletes in the downhill range; and 4) the running speeds adopted in downhill competition are far lower than metabolically feasible, mainly because of safety reasons. If athletes wish to improve their performances in competitions alternating ascent and descent phases, they should pay greatest attention to the training of movement coordination during downhill running.

We are indebted to Marino Giacometti, President of the International Altitude Sport Federation, for invaluable help in the organization of this study.

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G. S. Roi is presently at Isokinetic Rehabilitation Center, Bologna, Italy.

REFERENCES


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